

Light and photosynthesis modelling

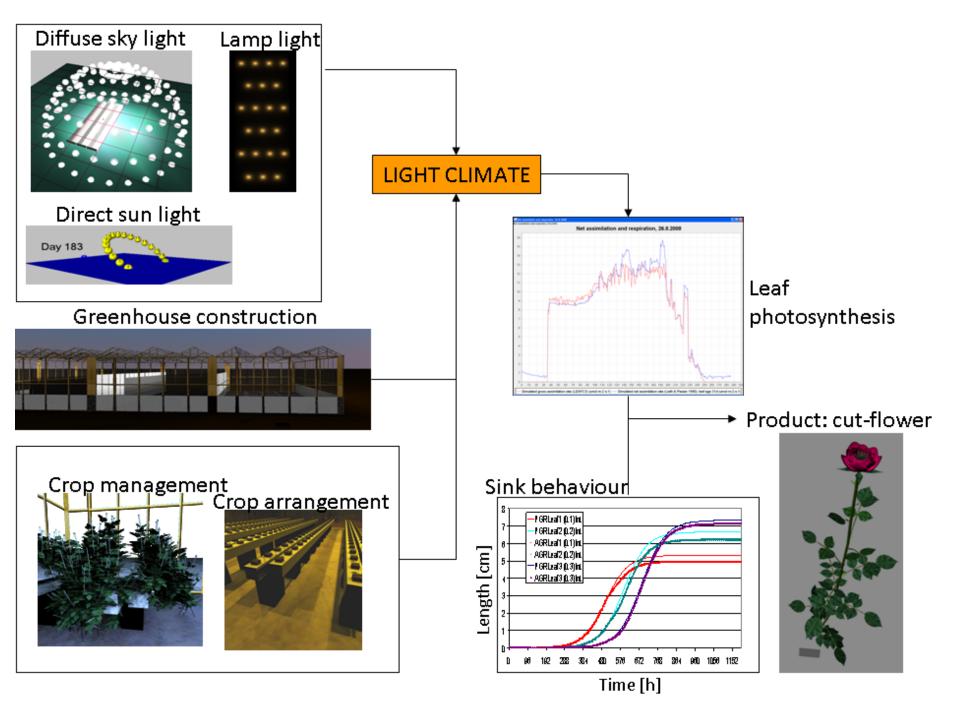
Time: 09:45 - 10:45

Presenter: Gerhard Buck-Sorlin & Michael Henke

Room: © CIP III

Summary

- Crop growth can be defined by five physiological determinants:
 - Light Interception, Light use efficiency, dry matter production and loss, duration of growth, and dry matter partitioning.
- Light interception can be modeled based on plant LAI in most cropping situations.
- Light use efficiency is a function of plant species.
- Dry matter production is a function of light interception and light use efficiency summed over the growth cycle of a plant.
- We can influence light interception by our choice of crops, row spacing, and planting geometry.



Light penetration into a homogeneous canopy, two approaches: 1) Homogeneous turbid medium → Lambert Beer's law

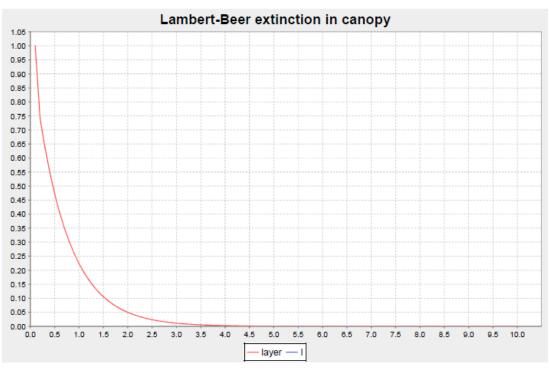
$$I_d = I_0 e^{-kd}$$

I = radiation level at canopy depth d

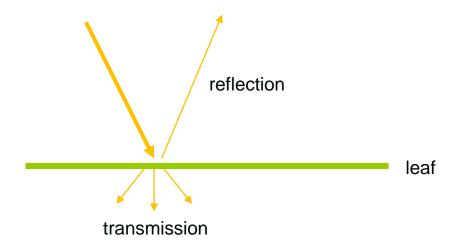
*I*₀: incoming radiation (above canopy)

k: extinction coefficient

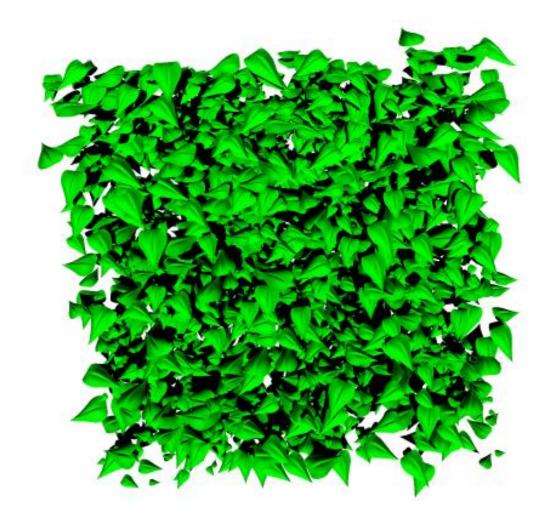
Demo simple layer model



Light absorption

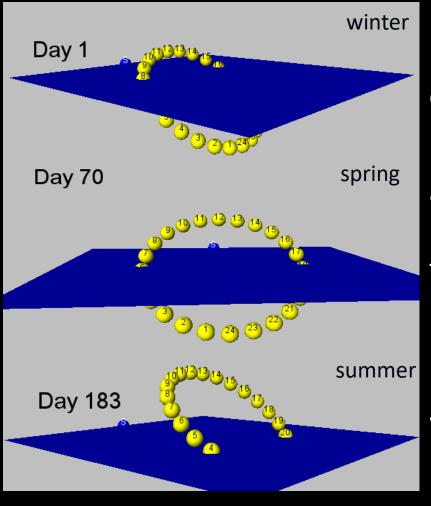


absorbed light = incident - reflected - transmitted light absorptance + reflectance + transmittance = 1 Light penetration into a homogeneous canopy, two approaches: 2) SAIL (Scattering by Arbitrarily Inclined Leaves) (Bunnik and Verhoef (1984)



Demo SAIL model

Modelling spatial light distribution: Daylight



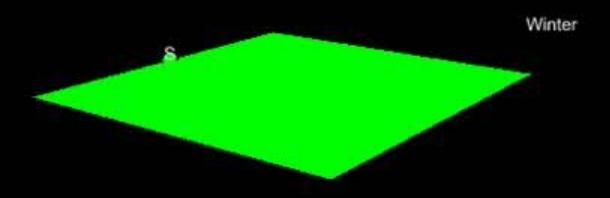
(Goudriaan 1994, modifié)

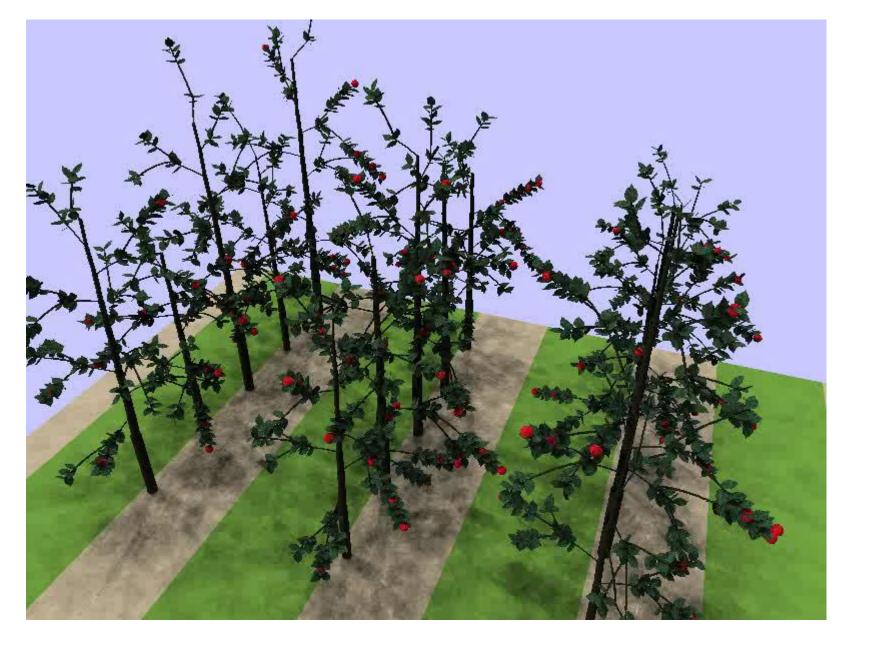
- input: latitude, day of year, time of day [h]
- simulation of direct sunlight as a directional light source (parallel rays), which changes position, thereby adjusting direction



• simulation of diffuse skylight with sky object (*Preetham et al. 1999*)

Sun Sky	
Channel input	Default
sun x	0.24523059
У	-0.32745484
z	0.9124885
turbidity	3.0
radianceFactor	254.2985



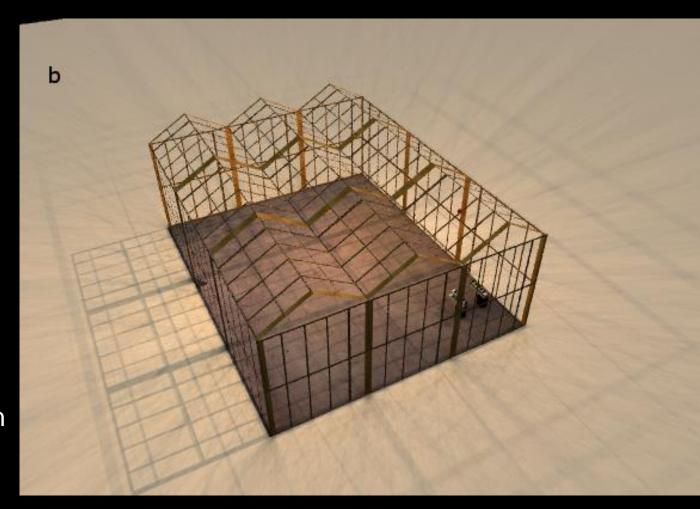


https://www.youtube.com/watch?v=FwZHEhz4hNM

Light distribution: Virtual greenhouse

View onto a virtual greenhouse simulated with the GroIMP platform

Lighting is simulated using 24 equally spaced SON-T assimilation lamps

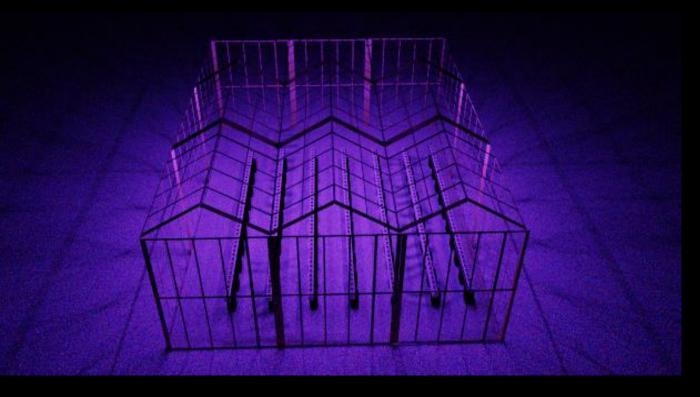


Buck-Sorlin et al. 2009







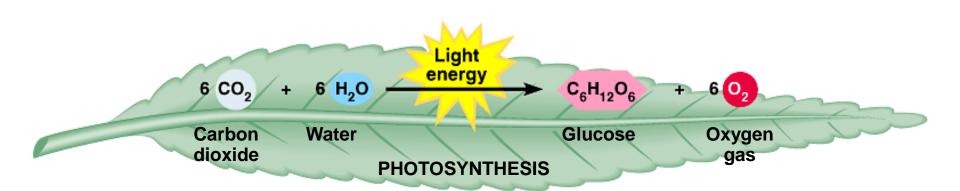




Modelling of photosynthesis

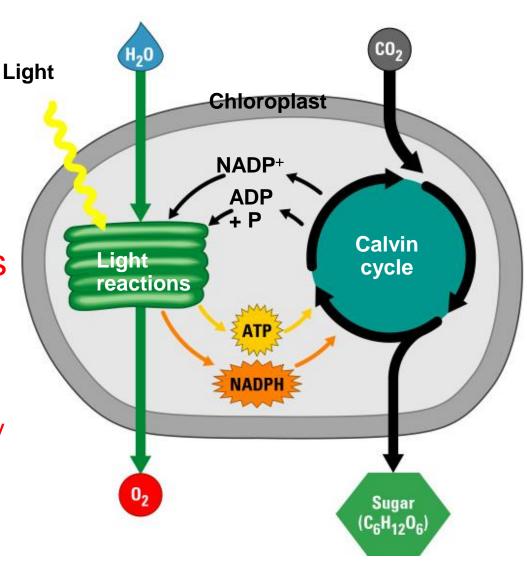
AN OVERVIEW OF PHOTOSYNTHESIS

 Photosynthesis is the process by which autotrophic organisms use light energy to make sugar and oxygen gas from carbon dioxide and water



AN OVERVIEW OF PHOTOSYNTHESIS

- The light reactions convert solar energy to chemical energy
 - Produce ATP & NADPH
- The Calvin cycle makes sugar from carbon dioxide
 - ATP generated by the light reactions provides the energy for sugar synthesis
 - The NADPH produced by the light reactions provides the electrons for the reduction of carbon dioxide to glucose



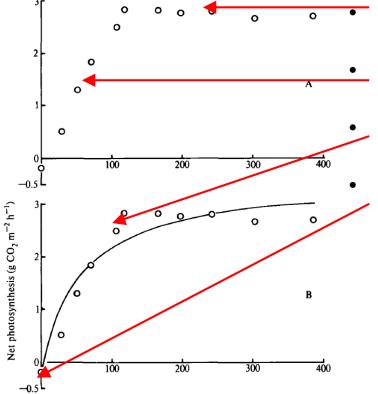
A first model of photosynthesis

- Blackman 1905: "When a process is conditioned as to its rapidity by a number of separate factors, the rate of the process is limited by the pace of the "slowest" factor".
- Five factors controlling assimilation recognized, of which three are easily measurable:
 - amount of CO₂ available,
 - amount of H₂O available,
 - intensity of available radiant energy,
 - · amount of chlorophyll present,
 - temperature in the chloroplast.
- Blackman's model describes a response of photosynthesis which increases linearly with irradiance (light-limited) until the available supply of CO₂ prevents further increase in the rate of photosynthesis with irradiance (CO₂-limited)

$$P=egin{cases} lpha I, & I\leq P_m/lpha, \ P_m, & I>P_m/lpha. \end{cases}$$

A first model of photosynthesis

- Rabinovitch (1951) proposed a number of alternative models, which were based on the *biochemical reactions* within the chloroplasts and used various simplifying assumptions to describe these complex reactions.
- The model proposed by Rabinowitch (1951) described the relationship between photosynthesis and irradiance in terms of a <u>rectangular hyperbola</u>



Above 100 W no increase in the net CO₂ exchange
⇒ saturation of the photosynthetic system by light.
Below 100 W m⁻² linear relationship between Pⁿ and irradiance.

only relatively small intermediate section of curvature → the 'shoulder'.

Point at zero irradiance measure of rate of dark respiration, R_d .

Rectangular Hyperbola

Thornley, 1976: A modification, appropriate for photosynthesis, of the model proposed by Michaelis and Menten for a simple enzyme-substrate reaction has been derived:

$$P_{g} = \frac{\alpha I \cdot (C_{f}/r_{x})}{\alpha I + (C_{f}/r_{x})}$$

$$\alpha = \text{photochemical efficiency}$$

$$I = \text{irradiance}$$

$$C_{f} = \text{CO}_{2} \text{ concentration at the site of}$$

where

 P_{g} = rate of gross photosynthesis

fixation

 $r_{\rm r}$ = chemical or carboxylation resistance.

Nonrectangular hyperbola

$$P_{n} = \frac{\alpha PAR + P_{g_{max}} - \theta R_{d} - \sqrt{\left(-(\alpha PAR + P_{g_{max}} - \theta R_{d})\right)^{2} - 4\theta\left(\alpha PAR\left(P_{g_{max}} - (1 - \theta)R_{d}\right) - R_{d}P_{g_{max}}\right)}}{2\theta}$$

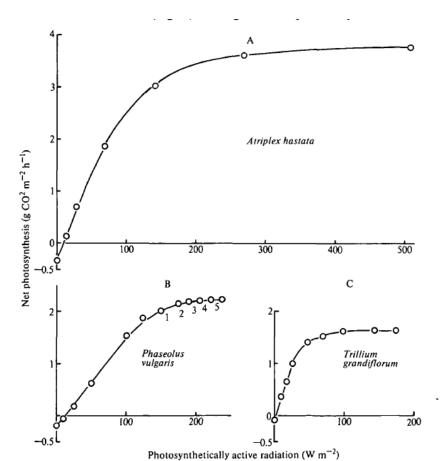


Fig. 3. Published curves for leaf net photosynthesis of C₃ plants in response to irradiance: (A) Bjorkman, 1975; (B) Chartier et al. (1970); (C) Taylor and Pearcy, 1976. The fitted curves were obtained from the photosynthesis—light response model.

where a = initial slope at zero irradiance and $\theta =$ ratio of physical to total resistance: describes the degree of curvature at the shoulder of the PLR.

Assuming that α , θ , P_{max} , and R_d are independent of irradiance, this equation describes the PLR as a <u>non-rectangular hyperbola</u>.

Marshall and Biscoe, 1980

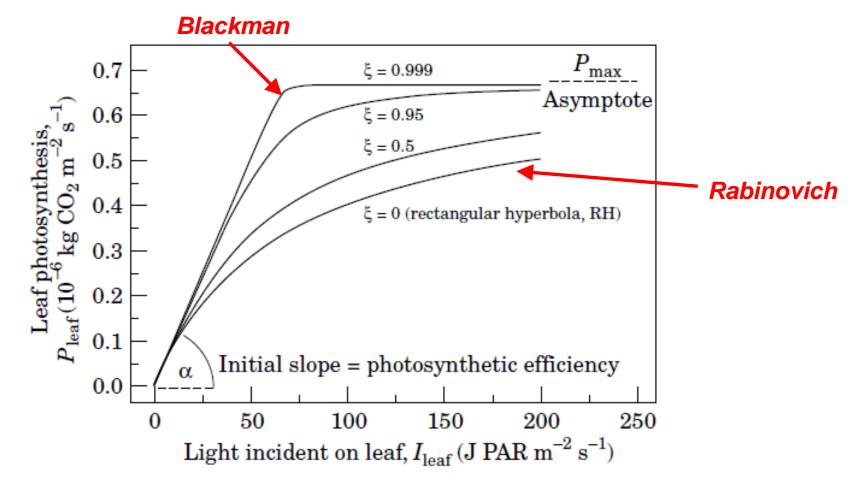


Fig. 1. Non-rectangular hyperbola for leaf photosynthesis. Equation (1) is plotted for $\alpha=1\times10^{-8}~{\rm kg~CO_2~J^{-1}}~[0.0494~\mu{\rm mol~CO_2}~({\rm mol~PAR})^{-1}],~P_{\rm max}=0.667\times10^{-6}~{\rm kg~CO_2~m^{-2}~s^{-1}}~(15~\mu{\rm mol~CO_2~m^{-2}~s^{-1}}).$ Four different values of the 'sharpness' parameter ξ are shown, with $\xi=0$ corresponding to the rectangular hyperbola. $10^{-6}~{\rm kg~CO_2}=23~\mu{\rm mol~CO_2}.~1~{\rm J~PAR}=4.6~\mu{\rm mol~PAR}.$

A biochemical photosynthesis model

$$W_c = V_{\rm m} \frac{C_{\rm i} - \Gamma}{C_{\rm i} + K}$$

$$W_{j} = J \frac{C_{i} - \Gamma}{4.5C_{i} + 10.5\Gamma}$$

 W_c : Rubisco-limited gross photosynthesis rate [mmol m⁻² s⁻¹]

 W_i : light-limited gross photosynthesis rate [mmol m⁻² s⁻¹]

 V_m : maximum carboxylation rate [mmol m⁻² s⁻¹]

J: electron transport rate [mmol m⁻² s⁻¹]

 C_i : intercellular CO_2 concentration [ppm or Pa]

 Γ : CO₂ compensation point without dark respiration

K: function of enzyme kinetics

Net CO₂ assimilation rate:

$$A = \min(W_c, W_j) - R_d$$

 R_d = daytime leaf dark respiration

Stomatal conductance

Ball et al. (1987) and Ball (1988) proposed a semi-empirical equilibrium model of stomatal conductance based on a number of gas exchange experiments with C3 and C4 plants, i.e.

$$g_{sv} = mA_n \frac{h_b}{c_b} + b_{sv}$$

With m = composite sensitivity of g_{sv} to net CO_2 assimilation (A_n) (species-specific, non-dimensional) and relative humidity (h_b) and CO_2 concentration (c_b) at the leaf surface, i.e. within the leaf boundary layer (h_b) is a decimal fraction, and c_b is a mole fraction). For C3 plants, m varies between 8 and 16 (Ball, 1988).

 b_{sv} = stomatal conductance that remains unaffected by the atmospheric environment or leaf biochemistry.

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A Coupled Model of Photosynthesis, Stomatal Conductance and Transpiration for a Rose Leaf (Rosa hybrida L.)

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The following three models were combined to predict simultaneously photosynthesis, stomatal conductance, transpiration and leaf temperature of a rose leaf: the biochemical model of photosynthesis of Farquhar, von Caemmerer and Berry (1980, Planta 149: 78–90), the stomatal conductance model of Ball, Woodrow and Berry (In: Biggens J, ed. Progress in photosynthesis research. The Netherlands: Martinus Nijhoff Publishers), and an energy balance model. The photosynthetic parameters: maximum carboxylation rate, potential rate of electron transport and rate of triose phosphate utilization, and their temperature dependence were determined using gas exchange data of fully expanded, young, sunlit leaves. The stomatal conductance model was calibrated independently. Prediction of net photosynthesis by the coupled model agreed well with the validation data, but the model tended to underestimate rates of stomatal conductance and transpiration. The coupled model developed in this study can be used to assist growers making environmental control decisions in glasshouse production.

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Key words: Rosa hybrida L., photosynthesis, stomatal conductance, transpiration, coupled model, cut-flower, crop simulation, calibration, validation.

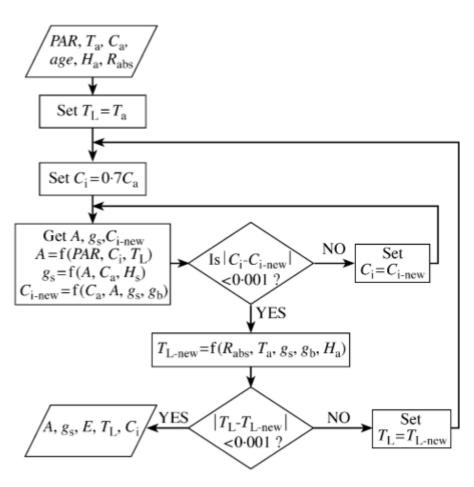


FIG. 1. Schematic diagram of the model flow.

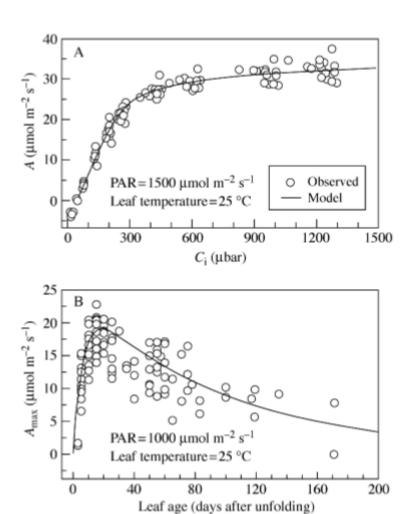


FIG. 2. Photosynthesis sub-model calibration. A, A/C_i response. Solid line represents the prediction of photosynthesis sub-model using measured C_i . B, Leaf age response of A_{\max} . Solid line represents the prediction of leaf age function.